

# CS5800: Algorithms — Spring '21 — Virgil Pavlu

Homework 9

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Name:

Collaborators:

Instructions:

- Make sure to put your name on the first page. If you are using the  $\text{\LaTeX}$  template we provided, then you can make sure it appears by filling in the `yourname` command.
- Please review the grading policy outlined in the course information page.
- You must also write down with whom you worked on the assignment. If this changes from problem to problem, then you should write down this information separately with each problem.
- Problem numbers (like Exercise 3.1-1) are corresponding to CLRS 3<sup>rd</sup> edition. While the 2<sup>nd</sup> edition has similar problems with similar numbers, the actual exercises and their solutions are different, so make sure you are using the 3<sup>rd</sup> edition.

1. (25 points) Exercise 17.3-3. (Hint: a reasonable potential function to use is  $\phi(D_i) = kn_i \cdot \ln n_i$  where  $n_i$  is the number of elements in the binary heap, and  $k$  is a big enough constant. You can use this function and just show the change in potential for each of the two operations.)

**Solution:**

2. (25 points) Exercise 17.3-6.

**Solution:**

3. (25 points) Exercise 19.2-1.

**Solution:**

4. (50 points) Implement binomial heaps as described in class and in the book. You should use links (pointers) to implement the structure as shown in the fig 1.

Your implementation should include the operations: Make-heap, Insert, Minimum, Extract-Min, Union, Decrease-Key, Delete

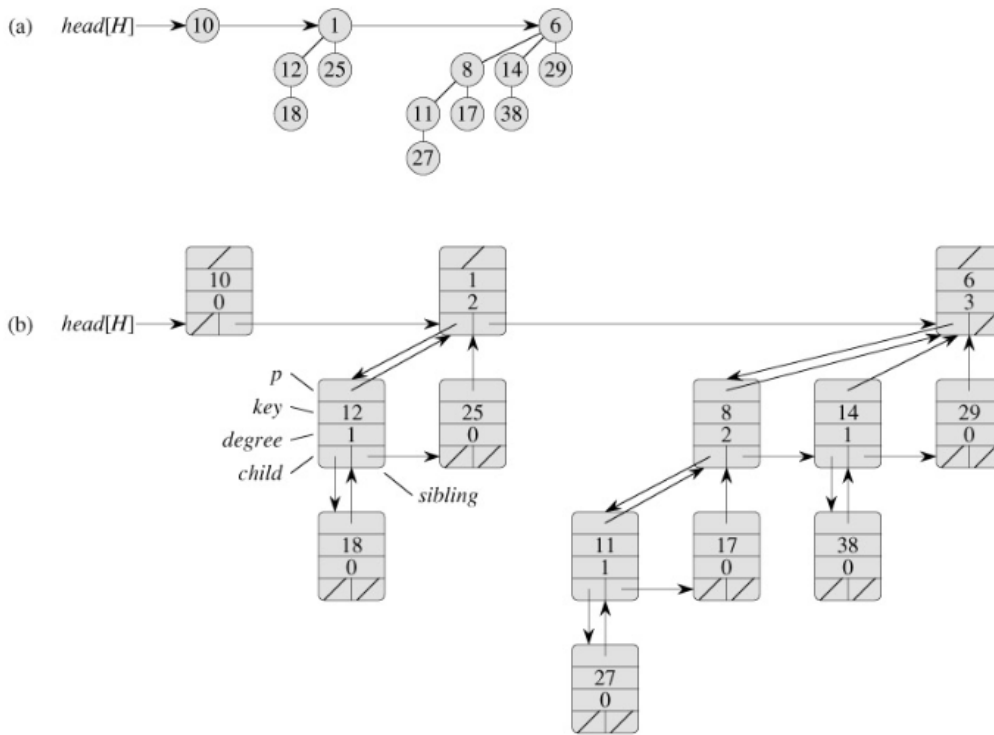


Figure 1: Binomial Heaps

Make sure to preserve the characteristics of binomial heaps at all times:

- (1) each component should be a binomial tree with children-keys bigger than the parent-key;
- (2) the binomial trees should be in order of size from left to right. Test your code several arrays set of random generated integers (keys).

**Solution:**

5. **(Extra Credit)** Find a way to nicely draw the binomial heap created from input, like in the figure.

**Solution:**

6. **(Extra Credit)** Write code to implement Fibonacci Heaps, with discussed operations: ExtractMin, Union, Consolidate, DecreaseKey, Delete.

**Solution:**

7. **(Extra Credit)** Figure out what are the marked nodes on Fibonacci Heaps. In particular explain how the potential function works for FIB-HEAP-EXTRACT-MEAN and FIB-HEAP-DECREASE-KEY operations.

**Solution:**