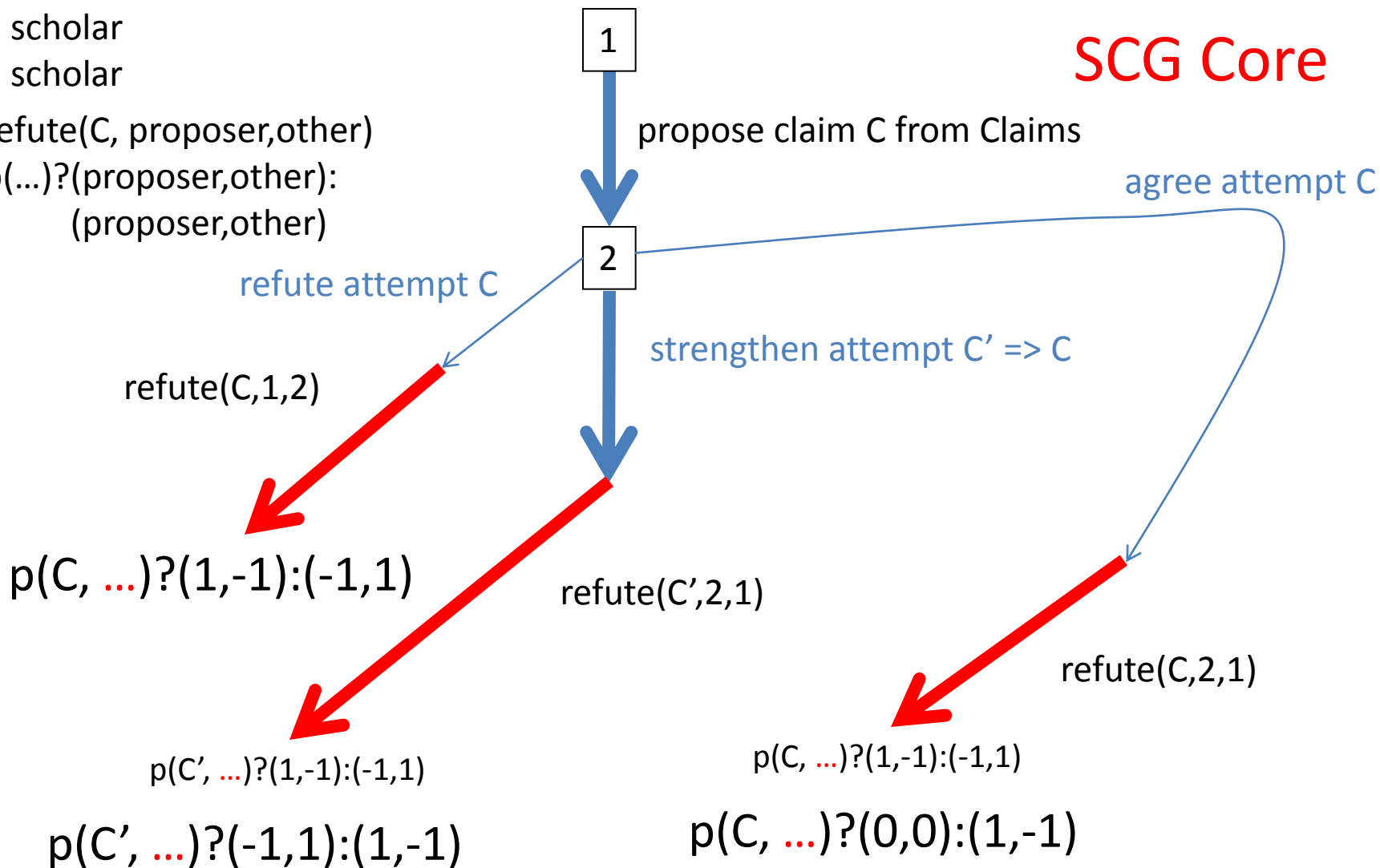


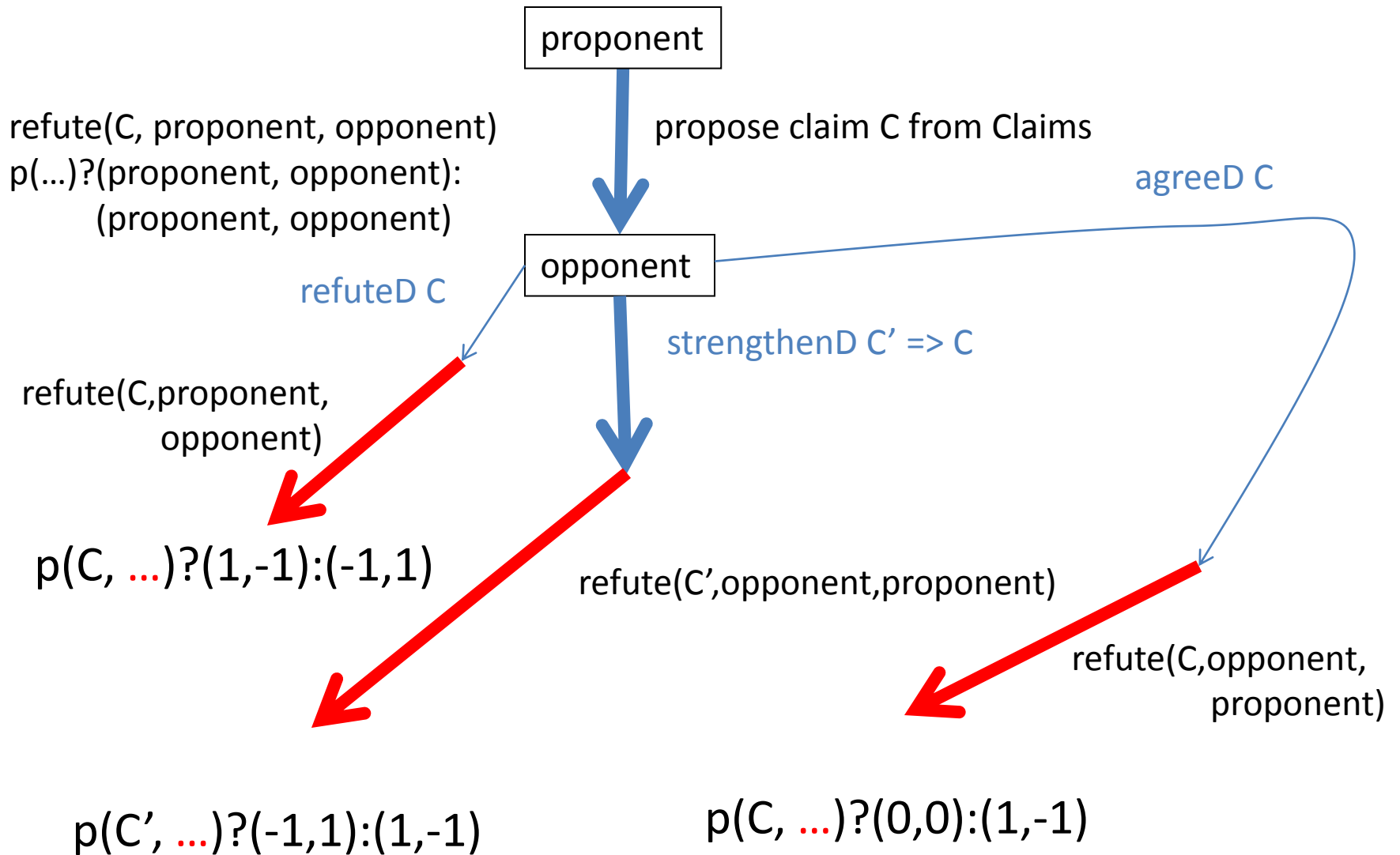
For Paper

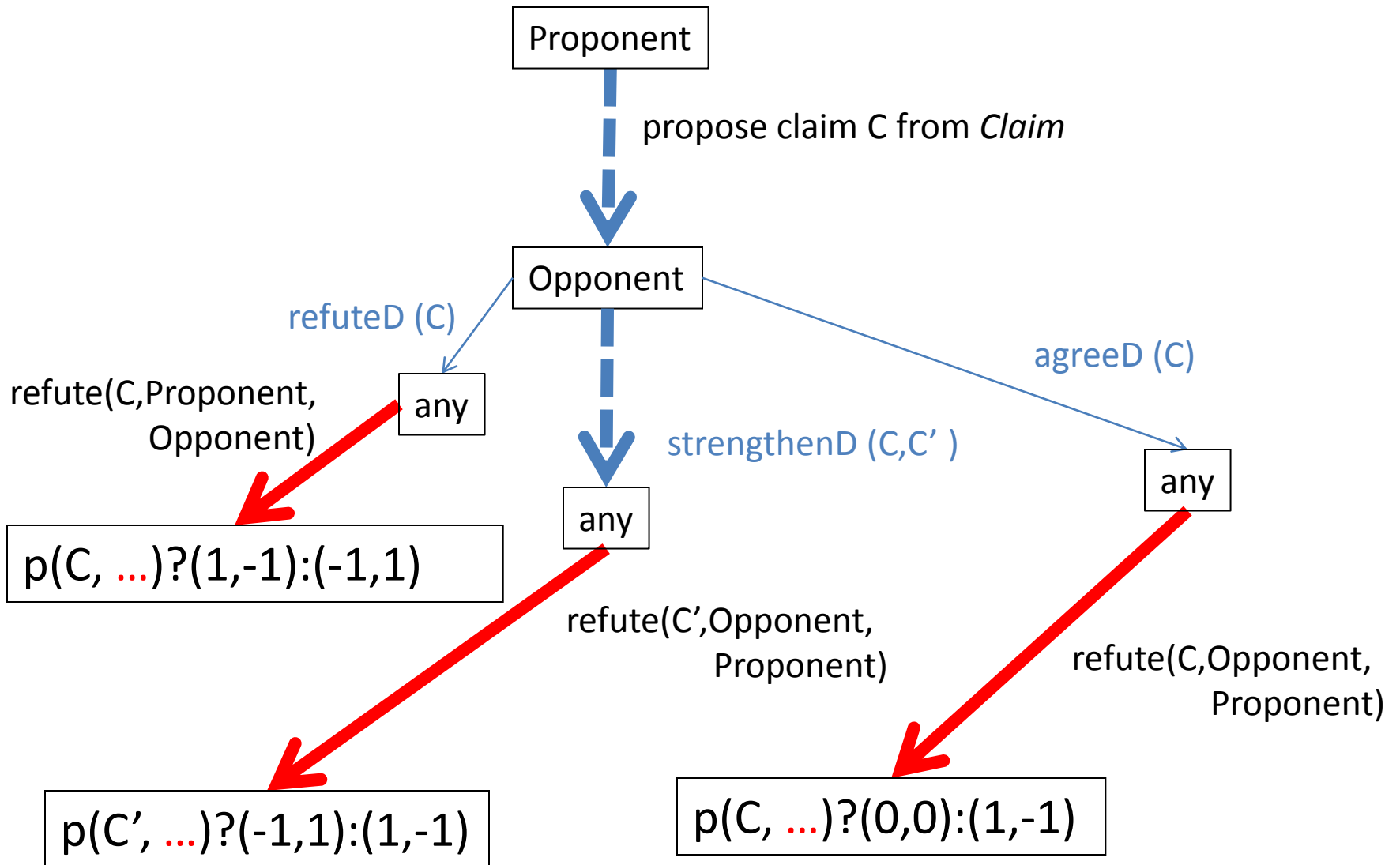
1 scholar
2 scholar

refute(C, proposer, other)
p(...)?(proposer, other):
(proposer, other)

SCG Core







Structures of SCG

Domain with name

Instance

Solution

valid(i: Instance, s: Solution

quality(i: Instance, s: Solution

Lab with name

d: Domain

claim parameter definitions

instance set predicate

refutation predicate

protocol

stronger(c1,c2: Claim)

distance(c1,c2: Claim)

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

Structures of SCG

Domain with name

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valid(i: Instance, s: Solution

quality(i: Instance, s: Solution

Example: calculus problem

SaddlePoint

Instance = [0,1]

Solution = [0,1]

valid(i,s) = true

quality(i,s) = $i*s + (1-i)*(1-s^2)$

Lab with name

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stronger(c1,c2: Claim)

distance(c1,c2: Claim)

SaddlePointLab

SaddlePoint

q: [0,1]

true

quality(i[0],s[1]) >= q

O:i[0], P:s[1] of i[0]

c1.q > c2.q

c1.q - c2.q

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

SPLClaim(

Alice,

SaddlePointLab,

0.6)

Structures of SCG

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distance(c1,c2: Claim)

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Example: worst-case of algorithm

GaleShapley (GS)

Nat

Preferences

valid(i,s) = s syntactically correct

quality(i,s) = GS iterations for s and i

GaleShapleyWorstCaseLab

GaleShapley

n:Nat, q: Nat

instanceSetP(i,n)=(i=n) //singleton

quality(i[0],s[1])>= q

O:i[0], P:s[1] of i[0]

c1.q>c2.q

c1.q-c2.q

GSWCLClaim(

Alice,

GaleShapleyWorstCaseLab,

10, 30)

Structures of SCG

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distance(c1,c2: Claim)

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Example: MaxSat

Satisfiability

CNF

Assignment

valid(i,s) = all variables in i assigned once

quality(i,s) = fraction of satisfied clauses in i

MaxSatLab

Satisfiability

q: [0,1], k: Nat (clause length)

instanceSetP(i,k)=clauses in i have length $\geq k$

quality(i[0],s[1]) $\geq q$

O:i[0], P:s[1] of s[0]

c1.q > c2.q

c1.q - c2.q

SJClaim(

Alice,

MaxSatLab,

$1 - (1/2^3), 3$)

Structures of SCG

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valid(i: Instance, s: Solution

quality(i: Instance, s: Solution

Lab with name

d: Domain

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distance(c1,c2: Claim)

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

Example: Boolean GeneralizedMaxSat = BMaxCSP

BooleanCSP

Sequence of Boolean constraints

Assignment

valid(i,s) = all variables in i assigned once

quality(i,s) = fraction of satisfied constraints in i

BooleanMaxCSPLab

BooleanCSP

q: [0,1], r: {R1,R2,...}

instanceSetP(i,r)=constraints in i use only r

quality(i[0],s[1])> =q

O:i[0], P:s[1] of s[0]

c1.q>c2.q

c1.q-c2.q

BMCLClaim(

Alice,

BooleanMaxCSPLab,

0.618, {R1,R2})

Structures of SCG

Domain with name

Instance

Solution

valid(i: Instance, s: Solution

quality(i: Instance, s: Solution

Lab with name

d: Domain

claim parameter definitions

instance set predicate

refutation predicate

protocol

stronger(c1,c2: Claim)

distance(c1,c2: Claim)

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

Example: BooleanMaxCSPLocalGlobal

BooleanCSP

Sequence of Boolean constraints

Assignment

valid(i,s) = all variables in i assigned once

quality(i,s) = fraction of satisfied constraints in i

BooleanMaxCSPLab

BooleanCSP

q: [0,1], r: {R1,R2,...}, k: Nat

instanceSetP(i,r,k)=(constraints in i use only r)

and any k constraints are satisfiable

quality(i[0],s[1])>=q

O:i[0], P:s[1] of s[0]

c1.q>c2.q

c1.q-c2.q

BMCLClaim(

Alice,

BooleanMaxCSPLab,

0.618, {R1,R2,R3,R4})

Structures of SCG

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quality(i: Instance, s: Solution

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distance(c1,c2: Claim)

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

Example: Solar Cells

SolarCells

RawMaterials

Product

valid(i,s) = only raw materials used

quality(i,s) = energy efficiency

SollarCellsLab

SollarCells

q: [0,1], k: Nat (raw material parameter)

instanceSetP(i,k)= ...

quality(i[0],s[1])> q

O:i[0], P:s[1] of s[0]

c1.q>c2.q

c1.q-c2.q

SCLClaim(

Alice,

SolarCellsLab,

0.7, 3)

expression in a, d, n using multiplication, addition and division.

To simplify, replace $(1+2+ \dots +n)$ by $n*(n+1)/2$.

$$\sum_{k=1}^n a + dk = (a + d) + (a + 2d) + (a + 3d) + \dots + (a + nd) = na + (1 + 2 + 3 \dots + n)d$$

Structures of SCG

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distance(c1,c2: Claim)

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

Example: Arithmetic Sequences Sum

ArithmeticSequences2

triple a,d,n: Nat

expression in a,d,n

valid(i,s) = s uses +,*,/ and vars in i

quality(i,s) = 1 if s is correct

Structures of SCG

Domain with name

Instance

Solution

valid(i: Instance, s: Solution

quality(i: Instance, s: Solution

Lab with name

d: Domain

claim parameter definitions

instance set predicate

refutation predicate

protocol

stronger(c1,c2: Claim)

distance(c1,c2: Claim)

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

Example: Arithmetic Sequences Sum

ArithmeticSequences

expression in a,d,n: Nat uses +,*,/

assignment to a,d,n

valid(i,s) = i gives correct sum for s: relaxed

quality(i,s) = 1 iff valid(i,s) : strict

ArithmeticSequencesLab

ArithmeticSequences

none

singleton

quality(i[0],s[1])=1 true

O:i[0], P:s[1] of s[0]

false

0

ASLClaim(

Alice,

ArithmeticSequencesLab,

)

Structures of SCG

Domain with name

Instance

Solution

valid(i: Instance, s: Solution

quality(i: Instance, s: Solution

Lab with name

d: Domain

claim parameter definitions

instance set predicate

refutation predicate

protocol

stronger(c1,c2: Claim)

distance(c1,c2: Claim)

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

Example: Arithmetic Sequences Sum

ArithmeticSequencesInduction

$\text{sum}[k=1..n] 2+3k = 2n+3(n(n+1))/2$

sequence of steps: induction proof

$\text{valid}(i,s) = \text{proof } s \text{ is correct induction proof}$

$\text{quality}(i,s) = 1 \text{ iff } \text{valid}(i,s)$

ArithmeticSequencesInductionLab

ArithmeticSequencesInduction

equation

singleton

$\text{quality}(i[0],s[1])=1$

$O:i[0], P:s[1] \text{ of } s[0]$

false

0

ASLClaim3(
Alice,

ArithmeticSequencesInductionLab,

$\text{sum}[k=1..n] 2+3k = 2n+3(n(n+1))/2$)

Structures of SCG

Domain with name

Instance

Solution

valid(i: Instance, s: Solution

quality(i: Instance, s: Solution

Example: HighestSafeRung

HighestSafeRung

pair(n,k)

decision tree

valid(i,s) = s is correct for (n,k)

quality(i,s) = depth(s)

Lab with name

d: Domain

claim parameter definitions

instance set predicate

refutation predicate

protocol

stronger(c1,c2: Claim)

distance(c1,c2: Claim)

HighestSafeRungLab

HighestSafeRung

n,k,q

singleton

quality(i[0],s[1])<=q

O:i[0], P:s[1] of s[0]

c1.q>c2.q

c1.q-c2.q

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

HSRClaim(

Alice,

HighestSafeRungLab,

25,2,5)

Structures of SCG

Domain with name

Instance

Solution

valid(i: Instance, s: Solution

quality(i: Instance, s: Solution

Example: LeafCovering

LeafCovering

Set of trees. Set M=subset of GCP of trees.
witness (leaf in GCP) of non-coverage by M

valid(i,s) = s is correct for i

quality(i,s) = unused

Lab with name

d: Domain

claim parameter definitions

instance set predicate

refutation predicate

protocol

stronger(c1,c2: Claim)

distance(c1,c2: Claim)

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

Structures of SCG

Domain with name

Instance

Solution

valid(i: Instance, s: Solution

quality(i: Instance, s: Solution

Lab with name

d: Domain

claim parameter definitions

instance set predicate

refutation predicate

protocol

stronger(c1,c2: Claim)

distance(c1,c2: Claim)

Claim with name

proponent: Scholar

lab : Lab

claim parameter values

Example: LeafCovering

LeafCovering

LeafCoveringProblem : Set of trees. Set M=subs

Program

valid(i,s) = s is correct for i

quality(i,s) = unused

LeafCoveringLab

LeafCovering

m: Nat (size of M)

instanceSetP(i,m)= |i.M|=m

quality(i[0],s[1])<=q

O:i[0], P:s[1] of s[0]

c1.q>c2.q

c1.q-c2.q

HSRClaim(

Alice,

HighestSafeRungLab,

25,2,5)